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**Table 1 Measured gravity harmonic coefficients of Saturn (un-normalized; reference radius 60330 km) and total ring mass (in units of Mimas' mass).**

The  $J$  value includes a constant tidal term owing to the average tidal perturbation from the satellites. The associated uncertainties are recommended values to be used for analysis and interpretation. For the zonal harmonics they correspond to 3 times the formal uncertainties. The solution for the total ring mass (A+B+C) is stable independently of the adopted dynamical model (table S2) and the uncertainty reported is the  $1\sigma$  formal uncertainty. See table S2 for our total ring mass estimates for several models of the unknown accelerations.

	Value	Uncertainty
$J_2$ ( $\times 10^6$ )	16290.573	0.028
$J_3$ ( $\times 10^6$ )	0.059	0.023
$J_4$ ( $\times 10^6$ )	-935.314	0.037
$J_5$ ( $\times 10^6$ )	-0.224	0.054
$J_6$ ( $\times 10^6$ )	86.340	0.087
$J_7$ ( $\times 10^6$ )	0.108	0.122
$J_8$ ( $\times 10^6$ )	-14.624	0.205
$J_9$ ( $\times 10^6$ )	0.369	0.260
$J_{10}$ ( $\times 10^6$ )	4.672	0.420
$J_{11}$ ( $\times 10^6$ )	-0.317	0.458
$J_{12}$ ( $\times 10^6$ )	-0.997	0.672
Ring mass ( $M_M$ )	0.41	0.13

**Table 2 Comparison of observed and calculated gravitational harmonics (un-normalized; reference radius 60330 km).**

Where two values are given they denote the minimum and maximum values from the suite of models. The physical models in column 3 match the observed  $J_2$  and  $J_4$  in Table 1, over a parameter space considering ranges of  $S_{\omega}$ ,  $Y_{\omega}$ ,  $Z_{\omega}$ ,  $r_i$  and rotation periods from 10h32m44s to 10h47m06s. For the same span of rotation periods, column 4 reports a wider range from models that match only  $J_2$  and allow for density modifications assuming  $r_i = 0.2$ . For  $J_4$ - $J_{10}$ , the discrepancy between measurements and uniform rotation models is large for all models that assume uniform rotation. Column 5 shows a representative model with DR on cylinders and a deep rotation period of 10h39m22s that matches measurements from  $J_2$  to  $J_{10}$ .

	Measurements	Physical models with uniform rotation		Uniform rotation model with modified density profiles		Physical model with differential rotation
$J_2$	$16290.573 \pm 0.028$	16290.57		16290.57		16290.573
$J_4$	$-935.314 \pm 0.037$	-935.31		-990.12	-902.93	-935.312
$J_6$	$86.340 \pm 0.087$	80.74	81.76	75.69	90.42	86.343
$J_8$	$-14.624 \pm 0.205$	-8.96	-8.70	-10.26	-7.97	-14.616
$J_{10}$	$4.672 \pm 0.420$	1.08	1.13	0.97	1.33	4.677

**Table 3 Contribution to the higher gravity harmonics  $\Delta J_2$  and  $\Delta J_4$  resulting from differential rotation and thermal-wind optimization.**

The deviation (Column 1) is the difference between the measured  $J_2$  and  $J_4$  (Table 1) and the average of the computed values from the 11 CMS models with uniform rotation (Table 2). Two optimizations are shown: one without latitudinal truncation of the zonal flow, resulting in the reconstructed zonal wind profile shown in Fig. 4A and with a flow depth of 9363 km (Column 2), and the second with the flows truncated at latitude  $60^\circ$  (Fig. 4B) and a flow depth of 8832 km (Column 3). Columns 4 and 5 show the deviations calculated with the thermal-gravity equation (48) for similar wind profiles. The solutions from thermal wind are closer to the measurement because the optimization was done using the thermal wind method, but the thermal-gravity solutions also match the observations within 10%.

	<b>Deviation</b>	<b>Thermal-wind solution</b>	<b>Thermal-wind solution truncated at latitude <math>60^\circ</math></b>	<b>Thermal-gravity solution</b>	<b>Thermal-gravity solution truncated at latitude <math>60^\circ</math></b>
$\Delta J_2$	$-5.600 \pm 0.205$	-5.624	-5.533	-5.758	-5.759
$\Delta J_4$	$3.528 \pm 0.659$	3.570	3.660	3.974	4.037